



# On the passive pitching mechanism in turning flapping flights using a torsional spring model

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## Abstract

In this work, we propose a three-dimensional passive pitching model of a flapping wing in pure yaw turn maneuver. The flapping and deviation motions are prescribed, but the interaction among the torsional spring, aerodynamic torques, and inertia torques governs the pitching motion. The aerodynamic forces and the unsteady flow are simulated by an in-house immersed-boundary-method based computational fluid dynamics (CFD) solver. The ratio of yaw angle rotation velocity to flapping velocity range from 0 to 0.25 are simulated with  $Re=300$  and stroke amplitude  $\phi = 120^\circ$ . The simulation results indicate the yaw angle rotation has significant impacts on both the aerodynamic performance and vortex structure. Specially, the yaw angle rotation strengthens the leading-edge vortex (LEV) of the wing and maintains a longer period for high angle of attack during the half-stroke in which flapping direction is same as yaw turn direction. It is also found the yaw angle rotation makes kinematic and aerodynamic asymmetric and increases the lift generation by 10.4% at yaw angle rotation velocity to flapping velocity ratio is 0.25. The findings of this work indicate the passive pitching mechanism may have great impacts on flapping flyer maneuver.

Keywords: *insect flight, torsional spring, passive pitching, maneuver, lift, asymmetric pitching, computational fluid dynamics*

## Nomenclature

$A$	Wing area
$c$	Mid-chord length
AR	Aspect ratio
$C_D$	Instantaneous drag coefficient and cycle-averaged drag coefficient, respectively
$C_L$	Instantaneous lift coefficient and cycle-averaged lift coefficient, respectively
$C_p$	Pressure coefficient
$\omega_f$	Flapping velocity
$f$	Flapping frequency
$f_n$	Natural frequency
$K$	Elastic modulus of torsional spring
$M_{aero}$	Aerodynamic torque
$M_{elastic}$	Elastic generated
$M_{gravity}$	Torque generated by gravitational force
$Re$	Reynolds number
$\theta$	Pitch angle
$\phi$	Stroke angle
$\alpha$	Deviation angle
$\alpha_m$	Deviation amplitude
$\Omega$	Yaw angle rotation velocity

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## I. Introduction

Flapping-wing propulsion is the most common motion type in flying animals and insects. There has been substantial interest in such motion over past decades due to its high maneuverability and efficiency compared to fixed-wing flight and rotorcraft. Understanding the flapping kinematics control mechanism is necessary for the design of micro air vehicle (MAV). In flies, there exists a high torsional flexibility area in the narrow basal and short root region<sup>1,2</sup>, which can result in the passive pitching motion during flapping.

Tremendous research and studies have been done in passive pitching mechanism. The passive pitching motion is governed by the combination of elastic force of wing, the aerodynamics force and the moment inertia of the wing<sup>3,4</sup>. Ishihara et al.<sup>3</sup> investigated the passive pitching due to wing torsional flexibility and lift generation in dipteran flight, and demonstrated that enough lift could be produced to support the weight of some dipterans. Bergou et al.<sup>5</sup> calculated rotational power about the torsion axis is owing to aerodynamic and wing inertial forces and suggested that the aerodynamic and inertial forces are sufficient to pitch the wing without the aid of the muscles. Whitney et al.<sup>6</sup> have estimated aeromechanics of passive rotation in flapping flight using blade-element model and compared results with experiments on artificial wings. Granlund et al.<sup>7</sup> experimentally studied hovering motions of flat plates with a free-to-pivot hinge at the leading edge. Due to the low resistance of hinges, the plate rests against an incidence limiter during most of the translation stroke in each direction. It was also found that the plate produces a motion akin to normal-hover, but with delayed rotation. Wan et al.<sup>8</sup> numerically simulated a two-dimensional hinged plate with passive rotation. They found that as the stroke amplitude reduces, the averaged lift-to-drag ratio decreases. When the plate flaps with very small amplitude, the average lift can be negative. Ishihara et al.<sup>4</sup> pointed out that due to the affection of wing elastic, the timing of the wing's rotation during the stroke reversal can be adjusted. Dai, H. et al.<sup>9</sup> and Kang, C. et al.<sup>10</sup> got similar results that lift force of the wing can be strongly enhanced by about 30% by properly choosing frequency ratio. Wang, Z.J et al.<sup>11</sup> made a comprehensive comparison between experimental, quasi-steady and computational and the results showed strong agreement. As for the relationship between the kinematical characteristics of the pitching motion and lift force generation, some researchers have tried to explain it. Passive maintenance of angle of attack during translation in crane fly wing was studied in<sup>12</sup>.

However, the passive pitching mechanism during maneuver is still unclear. Wang, Z.J et al.<sup>13</sup> found that fruit fly applied the passive mechanism to generate maneuver using only slight active actuation. But it is unclear what's the influence of maneuver on passive pitching mechanism, especially how the maneuver affects the lift generation.

In this study, high-fidelity three-dimensional simulations are performed to study the aerodynamics of torsional spring model in maneuver motions. The influence of maneuver on passive pitching and lift force production is discussed. An outline of the chapters shown as follow: Sec. II shows the problem formulation of hinge-linked torsional spring model and kinematics. Sec. III describes the computational method, simulation setup The simulation results and analysis on aerodynamic performance and vortex structure are presented in Sec. IV. At last, the conclusions are given in Sec. V.

## II. Problem formulation

### A. Flapping kinematics of wing

Figure 1 shows a three-dimensional hinge-connected rigid wing with an implemented torsional spring model. The hinge location is defined as:

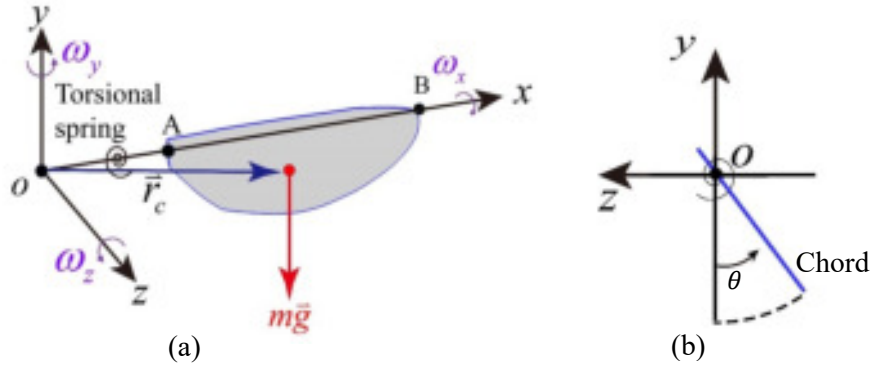
$$\mathbf{O} = \mathbf{A} - (\mathbf{B} - \mathbf{A}) \cdot \mathbf{r} \quad \text{Eq. (1)}$$

where  $\mathbf{O}$ ,  $\mathbf{A}$  and  $\mathbf{B}$  are the corresponding coordinates of points  $\mathbf{O}$ ,  $\mathbf{A}$  and  $\mathbf{B}$  shown in Eq. (1).  $\mathbf{r}$  is the hinge ratio. The wing shape is chosen to be same as the wing shape in experiment by Whitney and Wood<sup>6</sup>. Based on information provided, the distance from the rotation axis of the wing to the leading edge is 10% of the mid-cord length.

The flapping and deviation angles are prescribed which leaves us with only one degree of freedom of the wing namely, wing pitch. Flapping and deviation of the wing is given by Eq. (2),

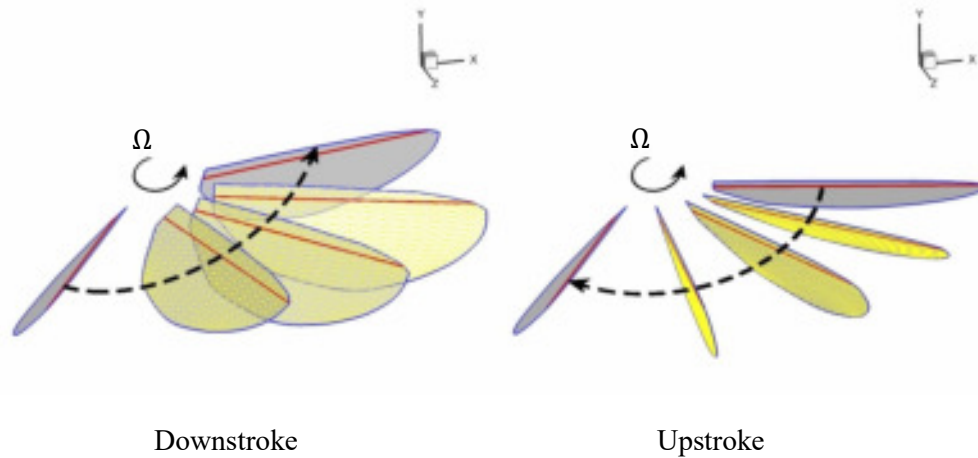
$$\begin{aligned}\phi(t) &= \phi_m \cos(2\pi ft + \pi) \\ \alpha(t) &= \alpha_m \sin(4\pi ft)\end{aligned}\tag{Eq. (2)}$$

where  $\phi$  and  $\alpha$  are the wing flapping and deviation angle, respectively.  $\phi_m$  and  $\alpha_m$  are the corresponding amplitudes of the two angles.  $f$  is the flapping frequency and  $t$  is the time.  $\theta$  is the pitching angle, which will be obtained by the simulation, and the angle of attack equals to  $90^\circ - |\theta|$ .



**Figure 1. The wing model used in the current study. (a) illustration of the main motion direction. Wing with a hinge (at point O). Oxyz is a non-inertial frame connected with the hinge of the flapping wing. The torsional spring is aligned with the ox axis.  $\omega_x$ ,  $\omega_y$  and  $\omega_z$  are the angular velocities around the x-, y- and z-axes. c is the center of mass of the wing.  $\vec{r}_c$  is the position vector of c in this local frame.  $m\vec{g}$  is the gravity respectively. (b) The definition of the pitch angle.**

To simulate maneuver motion, the body rotation  $\Omega$  is added to perform pure yaw turn in the present study. The yaw angle rotation velocity is chosen to be constant to simplify the problem. As shown in Fig.2, the prescribed flapping motion of wing with yaw turn is illustrated. The downstroke is defined as the half stroke when the flapping direction is same as the body rotation  $\Omega$ .



**Figure 2. Schematics of wing kinematics. The downstroke is defined as the half stroke when the flapping direction is same as the yaw turn direction.**

## B. Governing equation of a torsional spring wing model

The dynamic equation of the pitching motion can be written as,

$$I_{xx}\dot{\omega}_x + (I_{zz} - I_{yy})\omega_y\omega_z + I_{xy}(\dot{\omega}_x - \omega_x\omega_z) + I_{yz}(\omega_y^2 - \omega_z^2)\tag{Eq. (3)}$$

$$+I_{xz}(\dot{\omega}_z + \omega_x\omega_y) = M_{aero} + M_{elastic} + M_{gravity}$$

where  $I_{xx}$ ,  $I_{yy}$ ,  $I_{zz}$ ,  $I_{xy}$ ,  $I_{xx}$ , and  $I_{xz}$  are elements from the matrix of the moment of inertia of the wing.  $M_{aero}$ ,  $M_{elastic}$  and  $M_{gravity}$  are the torques due to aerodynamic, elastic, and gravitational forces, respectively.

The aerodynamic torque  $M_{aero}$  is obtained by the surface integration of pressure  $p$  and viscous stress tensor  $\sigma$ , it can be expressed as,

$$M_{aero} = \int_s (\sigma \cdot \vec{n} - p\vec{n}) \times \vec{r} ds \quad \text{Eq. (4)}$$

where  $\vec{n}$  is the outer normal to the body surface, and  $\vec{r}$  is the vector from mass center to certain surface element.

$$M_{elastic} = (K \cdot \theta) \vec{i} \quad \text{Eq. (5)}$$

where  $K$  is the elastic modulus and  $\vec{i}$  is the unit vector along the  $x$ -axis.

$$M_{gravity} = (\vec{i} \cdot (\vec{i}_c \times m\vec{g})) \vec{i} \quad \text{Eq. (6)}$$

where  $m$  is the mass of the wing.

### III. Numerical method

#### A. Computational method

The incompressible flow is governed by the Navier-Stokes equations, which can be written in tensor form as:

$$\frac{\partial u_i}{\partial x_i} = 0; \quad \frac{\partial u_i}{\partial t} + \frac{\partial u_i u_j}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \frac{1}{Re} \frac{\partial^2 u_i}{\partial x_i \partial x_j} \quad \text{Eq. (7)}$$

in which  $u_i$  ( $i=1,2,3$ ) is the velocity components, and  $p$  is the fluid pressure. Eq.(7) is solved by using finite-difference based Cartesian grid immersed boundary method<sup>14</sup>. A second-order central difference scheme in space is employed. Time is advanced using a second-order accurate fractional-step method. This method was successfully applied in many simulations of flapping propulsion<sup>15-23</sup>. More details about this method can be found in<sup>14,24</sup>. Validations about this solver can be found in our previous works<sup>25,26</sup>. The solver has great potential for solving more complex flow conditions and higher Reynolds numbers by adding structured adaptive mesh refinement (AMR)<sup>27,28</sup> in the future.

#### B. Simulation setup

In the present study, the non-dimensional parameters of Reynolds number are defined as follow,

$$Re = \frac{U_{tip} c}{\nu} \quad \text{Eq. (8)}$$

where  $U_{tip}$  is the non-dimensional wing tip velocity,  $c$  is the chord length, and  $\nu$  denotes the kinematic viscosity. The value of yaw angle rotation velocity is chosen based on Tyson L. Hedrick and Bo Cheng's study<sup>29</sup>. Different natural frequencies of spring range from 50Hz to 800Hz are simulated in hovering flapping motion, the simulation results indicate that the 150 Hz to 250 Hz is a good range in hovering flapping motion which can guarantee high efficiency and large lift force. Table 1 shows a summary of all the key parameters of the present study.

**Table 1. Key parameters of the present study**

$AR$	$Re$	$\phi$	$f_n/f$	$\Omega/\omega_f$
3.5	300	120°	1.5, 2, 2.5	0, 0.0625, 0.125, 0.1875, 0.25

where the  $\omega_f$  demotes flapping angular velocity with  $\omega_f = 2\pi f$ . The lift force coefficient  $C_L$  and drag force coefficient  $C_D$  are normalized by follows,

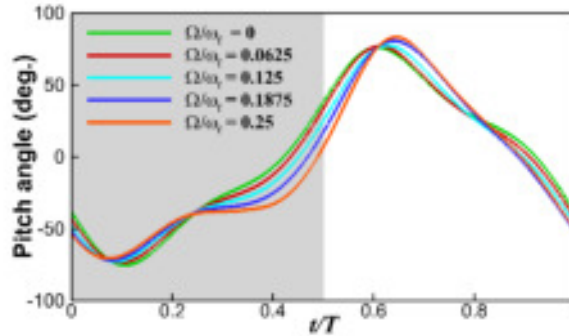
$$C_L = \frac{F_L}{\frac{1}{2}\rho U_{tip}^2 A}, \quad C_D = \frac{F_D}{\frac{1}{2}\rho U_{tip}^2 A} \quad \text{Eq. (9)}$$

The computational domain has the dimension of  $16c \times 16c \times 16c$  with  $205 \times 177 \times 205$  grids is designed in present study. A cuboidal region around the flapping wing with high resolution grids is designed to resolve the near-field vortex structures. The zero-gradient boundary condition is applied to all lateral boundaries and a homogeneous Neumann boundary condition is used for the pressure at all boundaries.

#### IV. Result and Analysis

In this section, the influence of pure yaw turn on aerodynamic performance and vortex structures are presented. A parametric study on the yaw velocity is presented to explore its influence on aerodynamic performance. The vortex evolution and shedding analysis are performed by comparing the instantaneous strength of leading edge vortex, tip vortex between the prescribed pitching motion case and the passive pitching case with same yaw velocity. The mechanism of pitch bump and asymmetric force production are discussed.

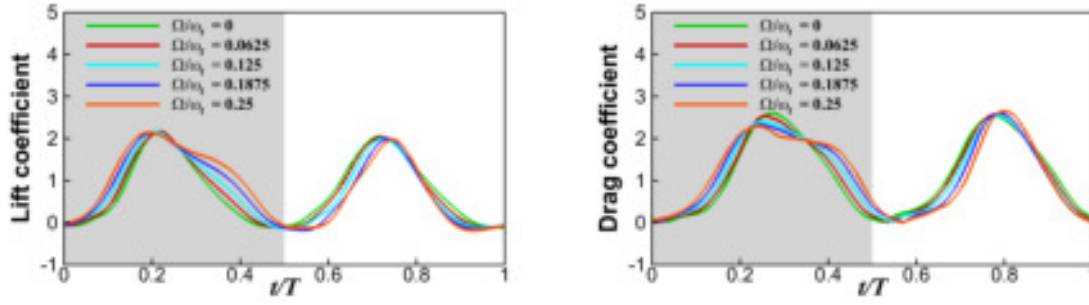
##### A. Overall comparison of aerodynamic performance of passive pitching cases with different yaw velocities



**Figure 3. Comparison of pitch angle with  $\phi = 120^\circ$  and  $\Omega/\omega_f = 0, 0.0625, 0.125, 0.1875$  and  $0.25$ , grey period is downstroke.**

The comparison of the pitch angle for a full stroke is shown in Fig.3. It can be observed that with the  $\Omega/\omega_f$  increases, the overall pitch angle behavior becomes more asymmetric. During downstroke, the pitch bump period which is immediately after the peak, becomes more obvious. The pitch angle changes relative slow during the pitch bump period. On the contrary, with the  $\Omega/\omega_f$  increases, the pitch bump becomes weaker during the upstroke. The timing of the pitch peak also influenced by the yaw turn. As the  $\Omega/\omega_f$  increases, the timings of the pitch peak shift forward in downstroke and it shift backward in upstroke. The time period between the pitch peaks in downstroke and upstroke at the  $\Omega/\omega_f = 0.25$  increases by about 20% compared to with the time period in case with  $\Omega/\omega_f = 0$ .

The instantaneous lift coefficient and drag coefficient are shown in Fig.4. It can be found that with the  $\Omega/\omega_f$  increases, the lift force and drag force production becomes asymmetric. The histories of the lift coefficient ( $C_L$ ) shows that there exists a bump during down-stroke from  $t = 0.3T$  to  $t = 0.5T$  and it doesn't show up in up-stroke. By comparing the bump start and end time instants with pitch angle in Fig.5, it can be concluded that the aerodynamic force production bump is related to pitch angle bump during this time period. As for the drag coefficient ( $C_D$ ), a similar force bump shows up but it starts at  $t = 0.4T$  and ends at  $t = 0.5T$ .



**Figure 4. Instantaneous lift coefficient ( $C_L$ ) and drag coefficient ( $C_D$ ) with  $\phi = 120^\circ$  and  $\Omega/\omega_f = 0, 0.0625, 0.125, 0.1875$  and  $0.25$ , grey period is downstroke.**

In Table 2 and Table 3 the cycle-averaged force coefficients with different  $\Omega/\omega_f$  are given. The mean lift force coefficient  $\bar{C}_L$  for each half stroke and mean drag force coefficient  $\bar{C}_D$  for each half stroke are given, also the averaged lift-to drag ratio, which characterizes aerodynamic performance. Based on the mean lift force coefficient data in Table 2, the  $\bar{C}_L$  increases with  $\Omega/\omega_f$  increases during down-stroke. On the other hand, the  $\bar{C}_L$  decreases with  $\Omega/\omega_f$  increases during up-stroke. But the mean value of whole stroke shows that with  $\Omega/\omega_f$  increases, the  $\bar{C}_L$  increases. The case with  $\Omega/\omega_f = 2.5$  shows 10.4% increasing of  $\bar{C}_L$  compared to the baseline case. when  $\Omega/\omega_f = 2.5$ , the drag force during down-stroke is about 44% higher than it during up-stroke. However, different from the lift force coefficient, the overall  $\bar{C}_D$  almost keeps the same as the baseline case. Comparing to the lift-to-drag ratio in Table 3, it can be observed that the passive pitching wing performs better with yaw turn angular velocity increases.

**Table 2. Cycle-averaged lift force coefficients with  $\phi = 120^\circ$  and  $\Omega/\omega_f = 0, 0.0625, 0.125, 0.1875$  and  $0.25$ .**

$\Omega/\omega_f$	$\bar{C}_L$	$\bar{C}_{L-downstroke}$	$\bar{C}_{L-upstroke}$
0	0.765 (baseline)	0.731	0.798
0.0625	0.767 (+0.2%)	0.815	0.719
0.1250	0.779 (+1.8%)	0.909	0.648
0.2875	0.793 (+3.6%)	1.018	0.567
0.2500	0.844 (+10.4%)	1.148	0.541

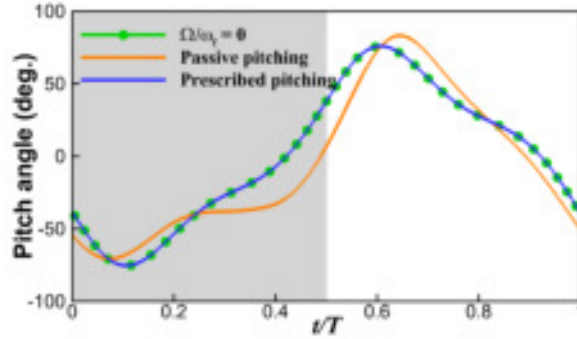
**Table 3. Cycle-averaged drag force coefficients with  $\phi = 120^\circ$  and  $\Omega/\omega_f = 0, 0.0625, 0.125, 0.1875$  and  $0.25$ .**

$\Omega/\omega_f$	$\bar{C}_D$	$\bar{C}_{D-downstroke}$	$\bar{C}_{D-upstroke}$	$\bar{C}_L/\bar{C}_D$
0	1.158 (baseline)	1.141	1.178	0.661 (baseline)
0.0625	1.156 (-0.20%)	1.197	1.117	0.664 (+0.05%)
0.1250	1.160 (+0.17%)	1.268	1.053	0.672 (+1.67%)
0.2875	1.167 (+0.78%)	1.337	1.004	0.678 (+2.57%)
0.2500	1.185 (+2.30%)	1.401	0.970	0.712(+7.72%)

## B. Comparison of performance between passive pitching and prescribed pitching motion.

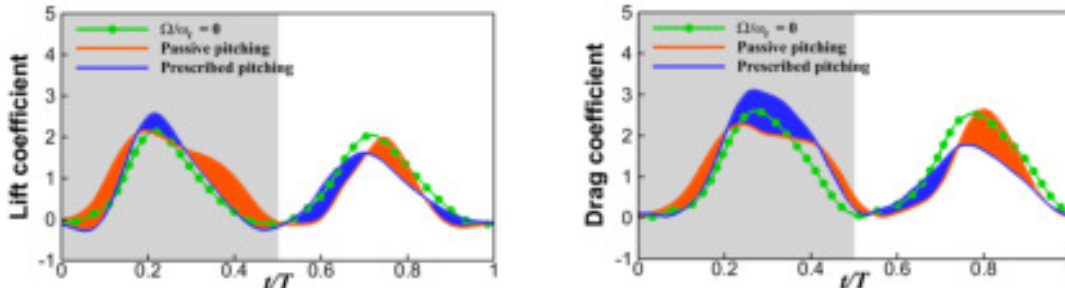
To better understanding the effects of passive pitching during maneuver, a prescribed pitching motion case is performed with  $\Omega/\omega_f = 0.25$ . The prescribed pitching motion is same as the pitching motion of passive pitching when the yaw velocity is zero. Therefore, the effects of passive pitching can be individually evaluated by comparing this prescribed pitching motion case with corresponding passive pitching case at same yaw velocity.

As shown in Fig.5, the pitch angle of passive pitching and prescribed pitching motion are presented. It can be found



**Figure 5. Comparison of pitch angle between passive pitching and prescribed pitching motion cases with  $\phi = 120^\circ$  grey period is downstroke.**

that the prescribed pitch angle is same as the pitch angle of passive pitching with  $\Omega/\omega_f = 0$ . The instantaneous force coefficient is presented in Fig.6, the major difference between passive pitching and prescribed pitching cases with  $\Omega/\omega_f = 0.25$  are colored. As it shows, the passive pitching case generates drag force relative earlier than prescribed pitching case and lasts relative longer time period during downstroke. But the peak value of drag force of passive pitching is much smaller than the prescribed pitching motion case. It might be because the pitch bump phenomenon due to passive pitching. As for the upstroke, the passive pitching case generates smaller drag force before mid-upstroke, but performs a larger drag force peak after mid-upstroke. The cycle-averaged force coefficients of these cases are shown in Table 4. When  $\Omega/\omega_f = 0.25$ , the lift coefficient of passive pitching case increases by 10.4% compared to passive pitching case with  $\Omega/\omega_f = 0$  while the prescribed pitching motion case decreases by 4.4%. As for the drag coefficient, both of these two cases increase by 2.2%. As a result, the passive pitching case has highest lift/drag ratio during maneuver among these three cases



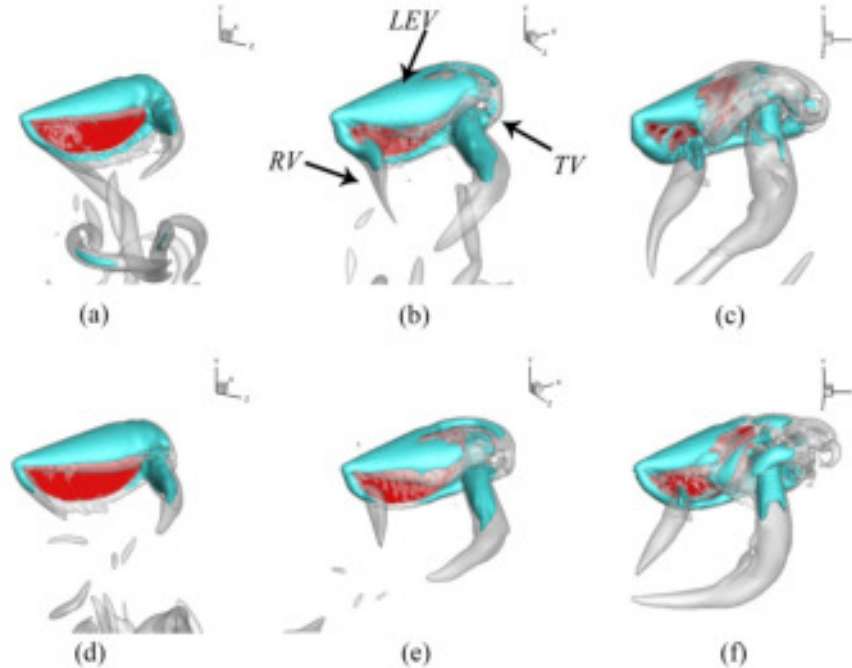
**Figure 6. Comparison of instantaneous lift coefficient ( $C_L$ ) and drag coefficient ( $C_D$ ) between passive pitching and prescribed pitching motion cases with  $\phi = 120^\circ$ , grey period is downstroke.**

**Table 4. Cycle-averaged force coefficients of passive pitching and prescribed pitching motion cases**

	$\bar{C}_L$	$\bar{C}_D$	$\bar{C}_L/\bar{C}_D$
$\Omega/\omega_f=0$	0.765 (baseline)	1.158 (baseline)	0.660 (baseline)
Prescribed pitching	0.731 (-4.4%)	1.185 (+2.2%)	0.617 (-6.5%)
Passive pitching	0.845 (+10.4%)	1.187 (+2.2%)	0.712 (+7.9%)

### C. Comparison of vortex structure between passive pitching and prescribed pitching motion cases of $\Omega/\omega_f = 2.5$

The three-dimensional flow structures of the passive pitching and prescribed pitching motion cases with  $\Omega/\omega_f = 0.25$  are visualized by plotting the iso-surface of the maximal imaginary part of complex eigenvalues of the velocity gradient tensor,  $\Lambda_{max}$ , which have been widely used in<sup>24</sup>. As shown in Fig.7, vortex formation during the down-stroke for the passive pitching and prescribed pitching motion cases are visualized with  $\Lambda_{max}=25$  for the outer surface and  $\Lambda_{max}=50$  for the core. To clearly present the three-dimensional flow structure at different time instant, the view is adjusted to make the wing keep a similar posture which makes comparison easier. Overall, the major flow structures in these two cases are similar but differences in vortex evolution and shedding can be observed, and these flow structures differences are highly related to the kinematics of wing. First, when  $t/T = 0.2$ , from (a) and (d), the LEV



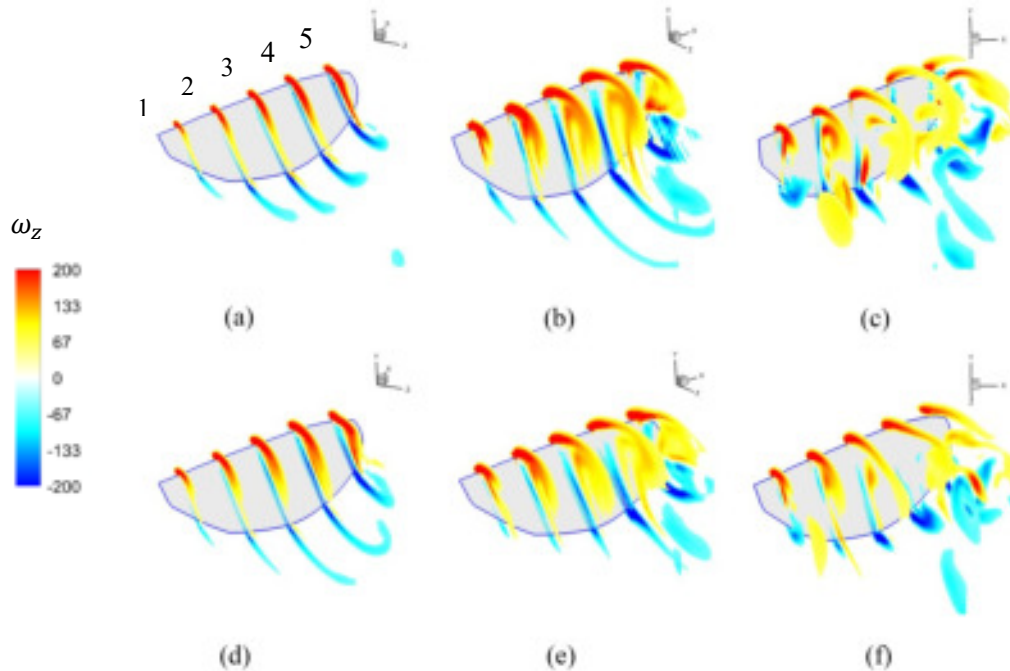
**Figure 7. Comparison of vortex structures between the prescribed pitching motion case with  $\Omega/\omega_f = 0.25$  at  $t/T =$  (a) 0.2, (b) 0.3, (c) 0.4. and the passive pitching case with  $\Omega/\omega_f = 0.25$  at  $t/T =$  (d) 0.2, (e) 0.3, (f) 0.4.**

forms along with the leading edge of the wing and it rises from the wing root to the position near wing tip, it can be found the passive pitching case has stronger LEV. The tip vortex (TV) is forms at the tip edge of the wing. When  $t/T = 0.4$ , for the passive pitching case, the TV becomes stronger and merges with some parts of LEV. As a result, partial LEV keeps attach on the wing surface and the rest of LEV transfers into TV. Combining with high pitch angle at this moment, it is consistent to the force production bump of this case. In comparison, in the prescribed pitching case, almost the whole LEV is going to shed which explains fast force drop during this period.

In Fig.8, slices of vorticity contours are plotted at  $t = 0.2T, 0.3T$  and  $0.4T$ . At the moement  $t = 0.2T$ , it can be seen from slice 1~5 that the strength of the LEV is slight stonger in the passive pitching case, which is consistent to the relative larger  $C_L$  and  $C_D$  value at this moment. The stonger LEV in (d) may due to the higher velocity gradient which leads to a larger shear layer forming a stronger LEV. When  $t = 0.3T$ , plot (e) shows the strength of LEV is stronger compared to that in plot (b). Moreover, the angle of attack in (b) becomes too large that results in large drag force while the angle of attack in (e) keeps a relative smaller value, that explains the relative higher instantaneous value of drag coefficient ( $C_D$ ) in Fig.6 at this moment. At the moement  $t = 0.4T$ , slices 1~3 in plot (f) shows that the LEV



still attach on wing surface only the LEV near wing tip detached while the LEV in (c) entirely shedded from the wing surface due to too large angle of attack.

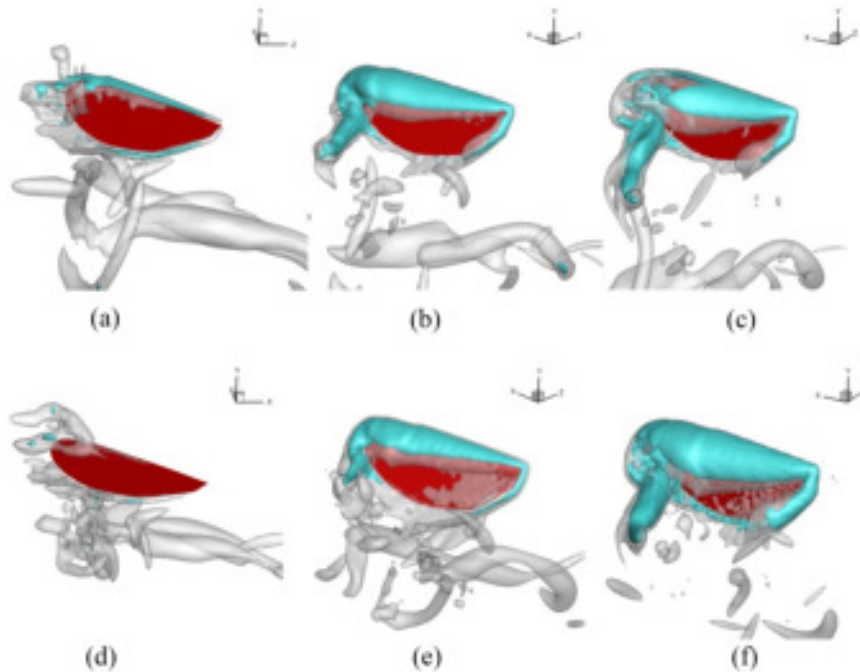


**Figure 8. Comparison of slices between the prescribed pitching motion case with  $\Omega/\omega_f = 0.25$  at  $t/T =$  (a) 0.2, (b) 0.3, (c) 0.4. and the passive pitching case with  $\Omega/\omega_f = 0.25$  at  $t/T =$  (d) 0.2, (e) 0.3, (f) 0.4.**

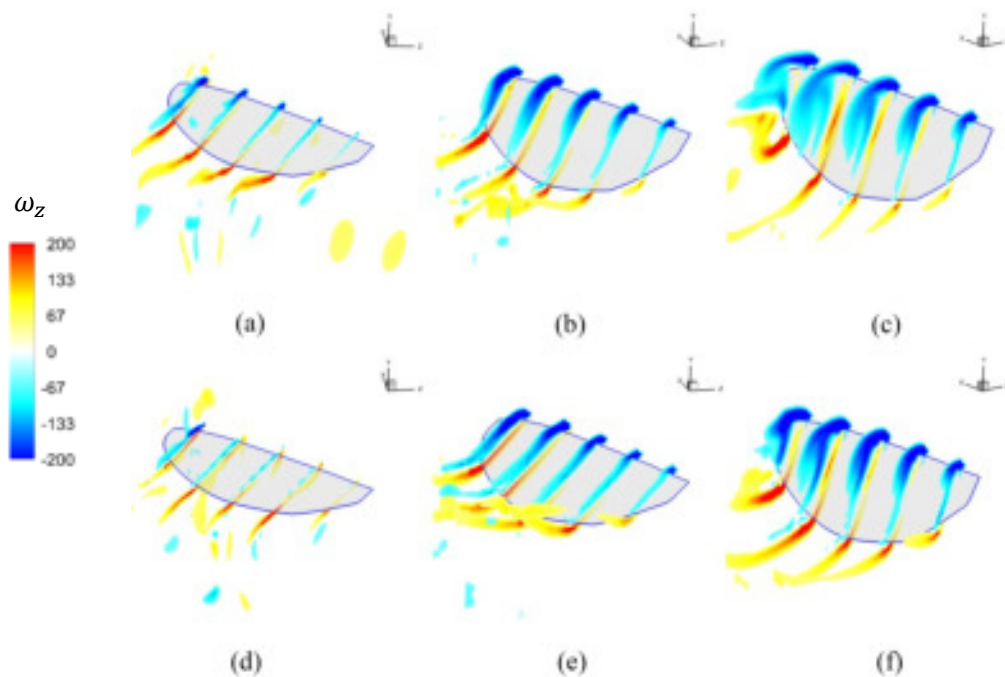
As for the upstroke, the three-dimensional flow structures are also visualized by the same setting as referred before. First, when  $t/T = 0.65$ , the passive pitching case doesn't generate LEV due to large pitch angle (small angle of attack) while prescribed motion case has a thin LEV on its wing surface. At  $t/T = 0.74$ , the prescribed motion case generates a stronger LEV compared to passive pitching which is consistent to the instantaneous force coefficient plot in Fig.6. when  $t/T = 0.8$  which is almost the end of upstroke, (c) shows that the LEV of prescribed pitching is going to detach from the wing surface. But the LEV of passive pitching case is strong at this moment.

To further understanding the vortex evolution, slices of vorticity contours of these moments are plotted in Fig.10. As it shows in the plot (c) and (f), the prescribed pitching motion case has significant LEV on its wing surface, but the LEV near wing tip is going to detach. As a comparison, the LEV of passive pitching case at this moment is relatively smaller but with a deeper color in the core area. That means the LEV of passive pitching case is stronger and steady attaches on the wing surface. Combining with pitching angle in Fig.5 and instantaneous force coefficient in Fig.6, the only difference between these two cases at this moment is the pitch angle changing rate, which means it might be because the faster pitching rotation leads to a stable LEV. Then, the passive pitching case has a relatively larger pitch angle compared to prescribed pitching case, that explains the larger drag force generation of passive pitching case during the end of the upstroke.

Combining discussion above, it can be concluded that during the downstroke, yaw velocity leads to a pitch bump in passive pitching which leads to a stronger LEV and lasts for longer time. As a result, the passive pitching case will have longer force generation period but smaller peak value. As for the upstroke, the yaw velocity results in a faster pitching changing rate which stabilizes the LEV from the mid-stroke to the end of the upstroke. As a consequence, the passive pitching case generates higher aerodynamic force peak amplitude compared to prescribed pitching motion.



**Figure 9.** Comparison of vortex structures between the prescribed pitching motion case with  $\Omega/\omega_f = 0.25$  at  $t/T =$  (a) 0.65, (b) 0.74, (c) 0.8. and the passive pitching case with  $\Omega/\omega_f = 0.25$  at  $t/T =$  (d) 0.65, (e) 0.74, (f) 0.80.



**Figure 10.** Comparison of slices between the prescribed pitching motion case with  $\Omega/\omega_f = 0.25$  at  $t/T =$  (a) 0.65, (b) 0.74, (c) 0.80. and the passive pitching case with  $\Omega/\omega_f = 0.25$  at  $t/T =$  (d) 0.65, (e) 0.74, (f) 0.80.

## V. Conclusion

In this study, we present a computational study of the fluid-body interaction of a rigid wing plate three-dimensional torsional spring model performing maneuver type of flapping motion. The passive pitching flapping model is modeled as a rigid wing plate with a torsional spring on wing root. The simulation shows that the aerodynamic performance and vortex structures of the wing can be greatly influenced by the yaw angle rotation.

With  $\Omega/\omega_f$  increases, the drag force generation during downstroke increases and it decreases during upstroke, and similar phenomenon also appears for lift force.

By comparing the passive pitching case with prescribed pitching motion case at yaw angle rotation velocity to flapping velocity ratio is 0.25. It is found that during the downstroke, the passive pitching case generates aerodynamic force for a longer period but has smaller peak value due to pitch bump. As for the upstroke, the passive pitching case generates aerodynamic force for a shorter period but has larger peak value due to the faster pitching rotation. It is found that the mean lift force generation of passive pitching case increases by 10.4% at yaw angle rotation velocity to flapping velocity ratio is 0.25 while the prescribed pitching motion case decreases by 4.4%.

Finally, in the present study, only one wing is simulated which limits study on yaw turn on passive pitching flapping. However, it is reasonable to believe that yaw turn will have similar but opposite influence on the other wing. In that case, the overall lift force of two wings will be maintained, or slightly increased during maneuver period. Also, based on our findings that the drag force difference between downstroke and upstroke of passive pitching become smaller compared to prescribed pitching motion case, which might have a significant influence on yaw turn of the flyer. It will be attractive to link such mechanisms to the maneuver of insects in the real world to understand the flow physics behind them.

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